Control and local measurement of the spin chemical potential in a magnetic insulator

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The spin chemical potential characterizes the tendency of spins to diffuse. Probing this quantity could provide insight into materials such as spin magnetic sensors and spin liquids and aid optimization of spintronic devices. Here we introduce single-spin magnetometry as a generic platform for nonperturbative, nanoscale characterization of spin chemical potentials. We experimentally realize this platform using diamond nitrogen-vacancy centers and use it to investigate magnons in a magnetic insulator, finding that the magnon chemical potential can be controlled by driving the system’s ferromagnetic resonance. We introduce a symmetry-based two-fluid theory describing the underlying magnon processes, measure the local thermomagnonic torque, and illustrate the detection sensitivity using electrically controlled spin injection. Our results pave the way for nanoscale control and imaging of spin transport in mesoscopic systems.

Control and measurement of the chemical potential of a spin system can be used to explore phenomena ranging from quantum phase transitions (1, 2) to Bose-Einstein condensation (3, 4) and spin transport in gases and solid-state systems (5–11). In recent decades, a large scientific effort has focused on harnessing spin transport for low-dissipation information processing (7, 12–14). In contrast to charge, spin is not a conserved quantity and naturally decays on the nanoscale for a wide range of materials, including typical metals (15, 16), calling for a local detection technique. Compared to the centuries-old techniques for studying charge transport, methods for probing spin chemical potentials have only been developed recently, with leading methods based on the coupling between spin and charge transport (6, 13, 14, 17) and inelastic light scattering (3, 18). Here we introduce a fundamentally different approach, which uses a single sensor spin to measure the local magnetic field fluctuations generated by a thermal spin bath. This approach is nonperturbative and provides spatial access to the spin chemical potential on a scale determined by the distance between the sensor spin and the system under study, opening the door to imaging spin transport phenomena with resolutions down to the few-nanometer scale.

Because the spin chemical potential is inherently related to spin fluctuations, it can be quantitatively determined by measuring the magnetic fields generated by these fluctuations. We demonstrate this principle using the excellent magnetic field sensitivity of the S = 1 electronic spin associated with the nitrogen-vacancy (NV) center in diamond (19, 20). We measure the chemical potential of magnons—the elementary spin excitations of magnetic materials (22)—in a 20-nm-thick film of the magnetic insulator yttrium-iron-garnet (YIG) on a ~100-nm-length scale (Fig. 1A). Our measurements reveal that the magnon chemical potential can be effectively controlled by exciting the system’s ferromagnetic resonance (FM) (Fig. 1, B and C).

Locally probing the weak magnetic fields generated by the fluctuations of a spin system requires nanometer proximity of a magnetic field sensor to the system. We ensure such proximity by positioning diamond nanobeam devices (21) that contain individually addressable NV centers onto the YIG surface (Fig. 1, D and E). We use a scanning confocal microscope to optically locate the NV centers and address their spin state (22, 23). A photoluminescence image (Fig. 1D) provides an overview of the system, showing an NV center (NV1) in a nanobeam that is located within a few micrometers from the gold and platinum striplines used to excite magnons in the YIG.

![Fig. 1. Local control and measurement of the magnon chemical potential. (A) Sketch of an NV spin locally probing the magnetic fields generated by magnons in a 20-nm-thick YIG film grown on a Gd$_3$Ga$_2$O$_{12}$ (GGG) substrate. (B) Sketch of the magnon dispersion and the magnon density, which falls off as $1/|E|$, as indicated by the fading colors, at zero chemical potential. (C) Driving at the FMR increases the magnon chemical potential. The NV spin probes the magnon density at the NV ESR frequencies $\omega_\text{m}$. (D) Photoluminescence image showing a diamond nanobeam containing individually addressable NV sensor spins positioned on top of the YIG film. A 600-nm-thick Au stripe (false-colored yellow) provides MW control of the magnon chemical potential and the NV spin states. A 10-nm-thick Pt stripe (false-colored gray) provides spin injection through the spin Hall effect. (E) Scanning electron microscope image of representative diamond nanobeam.](image-url)
Magnons generate a characteristic magnetic field spectrum reflecting the occupation of the magnon density of states. We probe this spectrum using the sensitivity of the NV spin relaxation rates $\Gamma_1$ to magnetic field fluctuations at the NV electron spin resonance (ESR) frequencies $\omega_n$ (Fig. 1, B and C) (28). For a system at thermal equilibrium, these rates can be expressed as (29)

$$\Gamma_1(\mu) = n(\omega_n, \mu) D(\omega_n, \mathbf{k}) f(\mathbf{k}, \mu) d\mathbf{k} + G_0^\infty$$

(1)

Here, $n(\omega_n, \mu) = \frac{\delta c}{\delta \mu}$ is the Rayleigh-Jeans distribution (which is the Bose-Einstein distribution in the high temperature limit appropriate for our room-temperature measurements), $\mu$ is the chemical potential, $k_B$ is Boltzmann’s constant, $T$ is the temperature, $\hbar$ is the reduced Planck’s constant, $D(\omega_n, \mathbf{k})$ is the magnon spectral density, $\mathbf{k}$ is the magnon wave vector, $f(\mathbf{k}, \mu)$ is a transfer function describing the magnon-generated fields at the NV site, $d$ is the distance of the NV to the YIG, and $G_0^\infty$ is an offset relaxation rate that is independent of the magnon spectrum. From Eq. 1, it is clear that, when $\Gamma_1(\mu) > G_0^\infty$, the chemical potential can be extracted in a way that is independent of many details of both sensor and system: Normalizing the relaxation rate measured at $\mu = 0$ by the relaxation rate measured at $\mu > 0$ yields

$$\mu = \hbar \omega_n (1 - \frac{\Gamma_1(0)}{\Gamma_1(\mu)})$$

(2)

As a first step in gaining confidence in this procedure, we probed the magnetic noise spectrum of the YIG film in the absence of external drive fields. We measured the NV spin relaxation rates as a function of an external magnetic field $B_{\text{ext}}$ applied along the NV axis [(23), fig. S4] and found excellent agreement with the model described by Eq. 1 (Fig. 2A). Qualitatively, the observed field dependence can be understood by noting the high density of magnons just above the FMR frequency, which induces a peak in the $m_s = 0 \leftrightarrow -1$ NV spin relaxation rate when the corresponding ESR frequency crosses this region (Fig. 2B), where $m_s$ labels the electron-spin eigenstate. A fit allows us to extract the distance of the NV to the YIG film (23). In extracting the NV relaxation rates, we assumed the direct relaxation rate between the $m_s = \pm 1$ states to be negligible, as this transition is spin forbidden and insensitive to magnetic noise.

Next, we studied the magnetic noise generated by the system under the application of a microwave (MW) drive field of amplitude $B_{\text{AC}}$ (23) using the sensitivity of the NV photoluminescence to magnetic fields at the ESR frequencies. Fig. 2C shows the photoluminescence of NV1 as a function of the drive frequency and $B_{\text{ext}}$. The straight lines result from the expected decrease in NV fluorescence when the drive frequency matches one of the NV ESR frequencies. In addition, the fluorescence decreases when the MW excitation frequency matches the calculated FMR condition of the YIG film. This effect results from an FMR-induced increase in the magnon density and associated magnetic field noise at the NV ESR frequencies (23, 25, 26). A line cut at $B_{\text{ext}} = 14.4$ mT shows a typical FMR linewidth of 8 MHz that we observe in these measurements (Fig. 2C, inset).

If the magnon occupation under the application of an FMR drive field can be described by the Rayleigh-Jeans distribution—as may be expected because magnon thermalization is driven primarily by the exchange interaction, which is by far the largest energy scale in our system (~THz)—Eq. 2 allows us to extract the chemical potential $\mu$ by measuring the NV relaxation rates. We measured the power dependence of the relaxation rate $\Gamma_1$ of NV1 at several values of the external magnetic field (Fig. 3A). We found that $\Gamma_1$ increases with drive power $B_{\text{AC}}^2$, consistent with the FMR-induced decrease of NV photoluminescence shown in Fig. 2C. Notably, $\Gamma_1$ saturates as a function of drive power; moreover, the corresponding chemical potential saturates exactly at the minimum of the magnon band set by the FMR (29) (Fig. 3B).

Because the band minimum is the maximum allowed value for the chemical potential of a boson system in thermal equilibrium (27), it provides a distinct reference point that is independent of any assumptions or experimentally unknown parameters. The precise match between the saturated value of the extracted chemical potential and the band minimum therefore underscores the validity of our method to extract the chemical potential.

We confirmed this saturation behavior using two different NV centers over a broad range of magnetic fields (Fig. 3, B and C), providing compelling evidence that the magnon density is described by a finite chemical potential in the spectral region probed in this measurement. We independently verified that the magnon temperature increases by less than 5 K at the highest drive power used in the measurements of Fig. 3B and does not significantly influence the extracted chemical potentials [see section S6 of (23)]. Another notable feature of our data is the initial slow increase of chemical potential observed at small $B_{\text{ext}}$ and low drive power (Fig. 3, B and D).

The build-up of chemical potential under the application of an FMR drive field can be understood as a pumping process of thermal magnons by the FMR-induced precession of the coherent...
spin order parameter $n$, where $n$ is a unit vector. An incoming thermal magnon scatters off the time-dependent $n$, generating two thermal magnons and transferring one unit of angular momentum from the coherent spin density to the incoherent spin density $\tilde{n}$ (23). This process is the Onsager reciprocal of a local thermomagnonic torque–induced precession of $n$ (27), which is gaining increased attention in the field of spin caloritronics. By using a two-fluid phenomenology (9), we can describe the mutual dynamics of $n$ and $\tilde{n}$ according to the following hydrodynamic equation (29)

$$\dot{\tilde{n}} = -\frac{\bar{\sigma}}{h^2} + \eta \cos \theta_n \frac{\bar{\sigma}}{n} (n \times n)$$  \hspace{1cm} (3)

Here, the first term on the right-hand side describes the decay of thermal magnons into the lattice, with $\bar{\sigma}$ a constant related to Gilbert damping. The second term describes the pumping of thermal magnons by the FMR-induced precession of $n$, with $\eta$ parametrizing the local thermomagnonic torque between $n$ and $\tilde{n}$ and $\theta_n$ parametrizing the instantaneous angle of $n$ with respect to the sample-plane normal $z$. By setting $\tilde{n} = 0$ and averaging the scalar triple product in Eq. 3 over a cycle of precession, under the assumption of the nonadiabatic pumping regime (23), we obtain

$$\mu = \frac{n}{\bar{\sigma}} \frac{\eta}{h^2} \cos^2 \theta_n$$ \hspace{1cm} (4)

where $\theta_n$ is the average magnetization angle with respect to the sample-plane normal $z$ and $\kappa$ is a parameter resulting from averaging over the elliptical motion of $n$.

A key prediction of this model, resulting from symmetry considerations (23), is that the coupling between $n$ and $\tilde{n}$ vanishes for an in-plane orientation of the magnetization (i.e., for $\theta_n = \pi/2$). We can test this prediction by using the measurement of the chemical potential as a function of $B_{\text{ext}}$ (Fig. 3D), as changing $B_{\text{ext}}$ changes $\theta_n$ in a well-defined way (29). We find that the dependence of the drive efficiency $d\mu/dB_{\text{AC}}$ on $B_{\text{ext}}$ in the low-power regime is accurately described by our theoretical prediction given by Eq. 4 (Fig. 3E), further supporting our conclusion that we are extracting the chemical potential correctly. We highlight that the precise knowledge of the in situ drive amplitude $B_{\text{AC}}$ provided by our NV sensor (23) is essential for this comparison. From a fit, we extract $\eta \approx 10^{-4}$ (23), which is comparable to the measured YIG Gilbert damping parameter $\alpha \approx 10^{-4}$ (28). According to the theoretical model studied in (29), $\eta$ describes the purely magnonic contribution to Gilbert damping and may thus be expected to be bounded by $\alpha$. The comparability of $\eta$ and $\alpha$ suggests that thermal magnons can exert a torque large enough to induce a magnetization precession.

Finally, we illustrated the power of our technique by characterizing the chemical potential that results from electrically controlled spin injection via the spin Hall effect (SHE). The SHE is a phenomenon originating from spin-orbit interaction, in which a charge current generates a transverse spin current. Such a spin current can be injected into a magnetic system, a technique widely used to study nonequilibrium magnon properties (14, 15, 17, 30, 31). Fig. 4A shows the measured relaxation rate of NV1 located ~17 $\mu$m from the edge of the Pt stripe line (Fig. 1D), as a function of the electrical current density $J$ in the Pt. We observed a clearly asymmetric dependence that is well described by a second-order polynomial (blue solid line)

$$\Gamma_- (\mu) = \Gamma_- (0) + \Gamma_1 + \Gamma_2$$  \hspace{1cm} (5)

with $\Gamma_1 \propto J$ the linear part and $\Gamma_2 \propto J^2$ the quadratic part.

Intuitively, we may expect the quadratic part of this polynomial to result from heating due to Ohmic dissipation in the Pt wire and the linear part to result from the SHE. We checked this expectation by exploiting the capability of the NV sensor to determine the temperature at the NV site through measurements of changes in the zero-field splitting of the NV spin states (23, 32). We assumed this temperature to be equal to the local YIG temperature because of the high thermal conductivity of diamond and the relatively insulating properties of air. We then used Eq. 1 to calculate the expected change in NV relaxation over the experimentally determined relevant temperature range of ~40 K (23). A comparison of this calculation with the data shows excellent quantitative agreement (Fig. 4B), illustrating the power of our technique.

**Fig. 3. Magnon chemical potential ($\mu$) under FMR excitation.** (A) NV1 relaxation rate $\Gamma_-$ as a function of the on-chip power $B_{\text{AC}}^2$ of a magnetic drive field applied at the FMR frequency, for different values of $B_{\text{ext}}$. The gray line is the fit from Fig. 2A, Top, measurement sequence. (B) $\mu$ as a function of $B_{\text{AC}}$ and $B_{\text{ext}}$. $\mu$ saturates at the minimum of the magnon band set by the FMR frequency. (C) Field dependence of the saturated value of the chemical potential $\mu_{\text{saturated}}$ calculated from averaging $\mu$ in the region $0.05 \text{ mT}^2 < B_{\text{AC}}^2 < 0.1 \text{ mT}^2$ [see (B)]. The black curve is the FMR. The red and blue points are measured by using the NV1, $m_s = 0 \leftrightarrow -1$ and NV2 $m_s = 0 \leftrightarrow +1$ transitions, respectively. $B_{\text{ext}}$ is oriented along the NV axis, at a $\theta = 65^\circ$ angle with respect to the sample-plane normal for both NVs and a $\phi = 52^\circ$ ($\phi = 67^\circ$) in-plane angle with respect to the Au stripe line for NV1 (NV2). The NV2 to YIG distance is $65 \pm 10$ nm (23). (D) At low $B_{\text{AC}}^2$, $\mu$ increases linearly at a rate $d\mu/dB_{\text{AC}}$ that depends on $B_{\text{ext}}$. (E) Field dependence of $d\mu/dB_{\text{AC}}^2$ extracted from (D). A comparison to theory yields the local thermomagnonic torque (see text). Fig. 3, A, B, and D, are shown with error bars in (23). In Fig. 3, C and E, the error bars are comparable to or smaller than the symbol size.
potential of NV spins for probing heat-related magnon phenomena, with applications in spin caloritronics, such as studies of the spin Seebeck effect (10, 11).

We attribute the linear part of the current-induced change in relaxation rate to a change in chemical potential induced by the SHE. Importantly, we rule out a possible influence of the Oersted field $B_{Oe}$ generated by the current in the Pt: We first use our NV sensor to measure $B_{Oe}$ in situ and then perform a control measurement of $\mu$, as a function of an externally applied field that mimics $B_{Oe}$ (23). We do not discern a significant effect of such a field on the NV relaxation rate (Fig. 4C). To extract the spin Hall–induced chemical potential from $\mu$, we expand Eq. 1 in the limit $\mu \ll \hbar \omega$ and assume a linear dependence $\mu \propto J_x$ (24, 25). We find that $\mu$ increases by $\sim 0.1$ GHz for $J_x = 1.2 \times 10^{11} \text{ A/m}^2$ (Fig. 4C). Furthermore, we find that for a given current through the Pt, $\mu$ does not significantly depend on the spectral detuning between $\omega$ and the FMR over a $\sim 35$-GHz frequency range, as determined by sweeping $B_{int}$ (Fig. 4D). In Fig. 4D, the spin-current injection efficiency is essentially constant, as the magnetization angle varies by less than $0.6^\circ$ (23).

Our results show that exciting the FMR provides an efficient mechanism to control the magnon chemical potential. Confined magnon resonances such as edge modes in ferromagnetic strips could serve as local sources of spin chemical potential to control spin currents. The ability to measure spin chemical potentials with an ultimate imaging resolution set by the NV-to-sample distance opens up new possibilities for measuring spin density, currents, and conductance in mesoscopic spin systems; exploring diffusive and ballistic spin transport; and aiding the development of new spintronic nanodevices.

REFERENCES AND NOTES

23. Materials and methods are available as supplementary materials.

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Diamonds to the rescue
Keeping track of spin transport inside a spintronic device is challenging. Du et al. came up with a method involving diamond nitrogen-vacancy (NV) centers, which can act like tiny, very sensitive magnetometers. The authors placed diamond nanobeams containing the NV centers in close proximity to the sample. This allowed them to measure the spin chemical potential of spin waves—so-called magnons—with nanometer resolution in the material yttrium iron garnet. Because NV centers are also sensitive to temperature, the method may be of use in spin caloritronics. Science, this issue p. 195

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